

Object recognition using eigenvectors

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ABSTRACT

A method for object recognition and pose estimation for robotic bin picking is presented. The approach discussed is a variant on current approaches to eigenimage analysis. Compared to traditional approaches which use object geometry only (shape invariants), the implementation described uses the eigenspace determined by processing the eigenvalues and eigenvectors of the image set. The image set is obtained by varying pose whilst maintaining a constant level of illumination in space, and the eigenspace is computed for each object of interest. For an unknown input image, the recognition algorithm projects this image to each eigenspace and the object is recognised using space partitioning methods which determine the object and the position in space. Several experimental results have been obtained to demonstrate the robustness of this method when applied to the robotic bin picking task.

Keywords: 3-D, bin picking, robot, eigenspace, object recognition, image set

2. INTRODUCTION

One of the main aims of an intelligent robotic vision system is to recognise objects and to compute their position in space. The vision recognition task must be performed as close to real time as possible. Therefore the recognition algorithm must be computationally inexpensive.

In this paper we present an approach based on the use of eigenvectors (eigenimage). This can be briefly described as a method, which computes the eigenspace determined by processing the eigenvalues and eigenvectors of the image set (see also [7], [8], [13], [16]). For our practical implementation in order to decrease the number of images, the image set is obtained by varying pose while maintaining a constant level of illumination. The eigenspace is determined using the eigenvalues (eigenvectors) of covariance matrix in order to obtain a low dimensional subspace. For an unknown input image, the recognition algorithm projects this image to eigenspace and the object is recognised using the space partitioning method, which determines the object and also its position in space according with the number of images that describe the position from the image set [6].

The image set is normalised in brightness and the background noise removed in order to eliminate the redundant information. The eigenspace for the image set is built by computing the biggest eigenvalues (eigenvectors) of the set. The next step is to project all the images onto eigenspace and we obtain a set of points that characterise the object and the pose in space. In order to increase the resolution for position estimation we connected these points in eigenspace and an unknown position can be better approximated. The first step could be considered by analogy with neural networks as “learning” and the recognition by space partitioning as “matching”.

In our approach we consider the objects from images are not occluded. Another important problem can be the texture reflectance and this problem is directly connected to the illumination conditions.

In comparison with other approaches based on geometry recognition (see also [1], [4], [14]) this method is suitable for a large number of objects with different shape geometry.

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3. CALCULATING EIGENSPACE

An image $I(x,y)$ is represented by a two-dimensional 256 by 256 array of 8-bit intensity values. This image can also be considered as a vector of dimension 65536. This is obtained by reading pixel brightness values in a raster scan manner.

To reconstruct an image we map a collection of points (in our case eigenvalues) in this huge space. The main idea of the principal component analysis (Karhunen-Loeve expansion) is to find the vectors that can better describe the image (or the entire space).

These vectors describe an orthonormal space and this property is presented below:

$$u_i u_j^T = \mathbf{g}_j = \begin{cases} 1, & \text{if } i = j \\ 0, & \text{if } i \neq j \end{cases} \quad (1)$$

where u_i, u_j are two eigenvectors and \mathbf{g}_j is the scalar product.

$$I = [i_1, i_2, i_3, \dots, i_N] \quad (2)$$

where i_1, i_2, \dots, i_N are the pixel values.

This vector represents an unprocessed image. The reflectance proprieties of the object shape can vary from scene to scene. If the illumination conditions of the environment are maintained constant, the appearance is affected only by object position.

The image set for an object is obtained as:

$$[I_1, I_2, I_3, \dots, I_P]^T \quad (3)$$

where P is the number of considered positions in space.

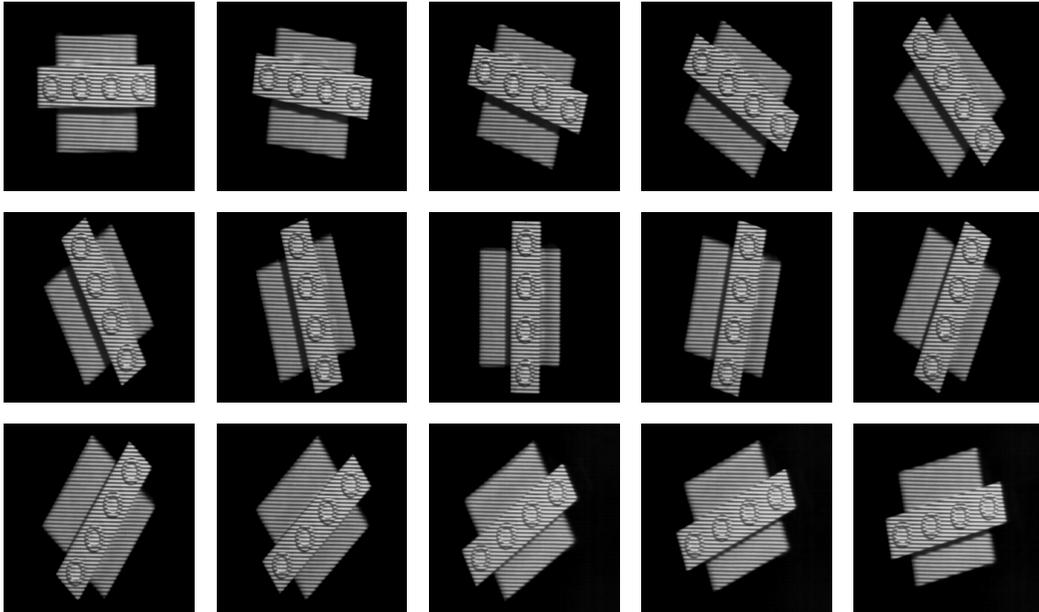


Figure 1. Image set obtained by rotating the object. All images are normalised for brightness.

Because we do not want our images to be affected by the variations in the intensity illumination or the aperture of the imaging system (lens), we normalise each image so that the total energy contained in the image is unity [6]. The normalised image is obtained by dividing each pixel by the following number:

$$i'_n = \frac{1}{B} i_n, \quad B = \sqrt{\sum_{n=1}^N i_n^2} \quad (4)$$

Before computing the eigenspace we need to calculate the average image (A) of all images:

$$A = \frac{1}{P} \sum_{i=1}^P I_i \quad (5)$$

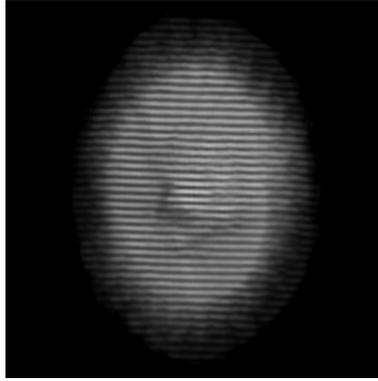


Figure 2. The average matrix for image set

The image set will be obtained by subtracting the average image (A) from each normalised image:

$$S = [I'_1 - A, I'_2 - A, I'_3 - A, \dots, I'_P - A]^T \quad (6)$$

The dimension of matrix S is $P \times N$, where P is the number of positions (images) and N the number of pixels. The next step involves the computing the covariance matrix:

$$C = S^T S \quad (7)$$

This matrix is very large (65536 x 65536) and it will be extremely difficult to compute the eigenvalues and the corresponding eigenvectors. If the number of images P is smaller than N it is easier to construct the P by P matrix $Q = SS^T$, but in this case the dimension of space is maximum P . The eigenvalues and the corresponding eigenvectors are computed solving the following well known equation:

$$Q u_i = v_i u_i \quad (8)$$

where u_i is the i^{th} eigenvector and v_i is the corresponding eigenvalue.

The eigenspace is obtained by multiplying matrix of eigenvectors (eigenmatrix) with the matrix S :

$$E = US \quad (9)$$

where $U = [u_1, u_2, \dots, u_P]^T$, U is $P \times P$ dimensional. As we expect the matrix E that represents the eigenspace is $P \times N$ dimensional.

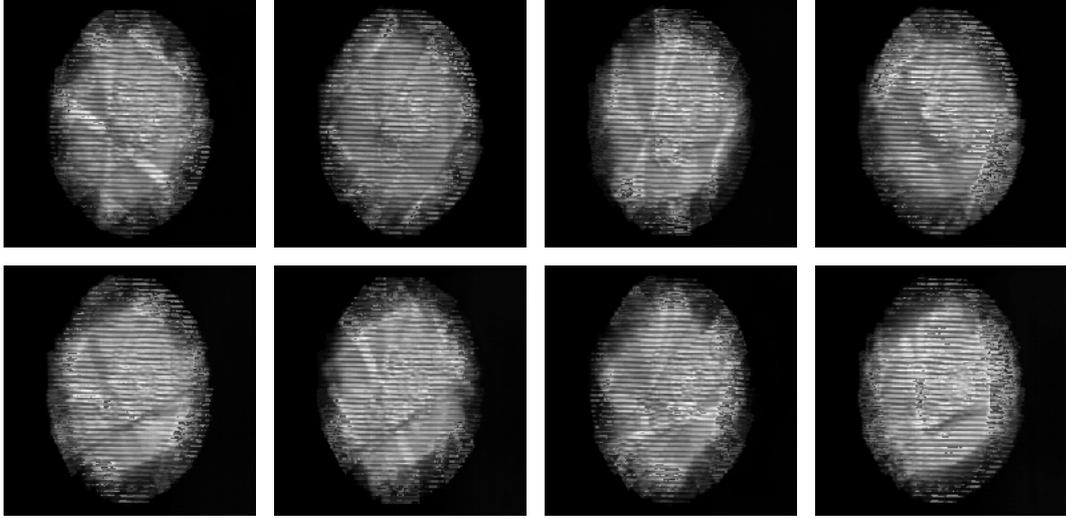


Figure 3. Eight of the eigenvectors corresponding to the largest eigenvalues calculated for the input image set

Using this approach the number of calculations is significantly reduced but in this case the number of eigenvectors is relatively small (up to 36). For an exact description we need N eigenvectors, but for recognition purpose a smaller number is sufficient to describe a low dimensional subspace.

4. OBJECT RECOGNITION AND POSITION ESTIMATION

Once the eigenspace is computed we can project all images from the set on this subspace ($E=[e_1, e_2, \dots, e_p]^T$). The result will be a collection of points that describe the object and its position. Before projecting the image set onto eigenspace, we subtract the average image from the image set.

$$h_i = [e_1, e_2, \dots, e_p]^T (I_i' - A) \quad (10)$$

where e_1, e_2, \dots, e_p are the eigenspace vectors and each vector is N dimensional.

As we expect each point is P dimensional and this appears to be a severe restriction in image reconstruction. But for the purpose of recognition, this allows us a fairly accurate method under the condition of maintaining a constant illumination. If these points are connected in P space to give us the possibility of estimating positions of the object that are not included in the image set. A direct connection between position of the object and the projection on the eigenspace (or object space) is obtained.

An unknown input image will be projected onto eigenspace and as result we will obtain a P dimensional point. This vector can be used in a standard recognition algorithm and the simplest method to determine the best matching is to compute the Euclidean distance [6], [15].

$$d_i^2 = \|h - h_i\|^2 = (h - h_i)^T (h - h_i) = h^T h - h_i^T h_i \quad (11)$$

where $i=1,2,\dots,P$ and h is the projection of the input image onto eigenspace.

We consider the recognition task to find the object and its position. The object is in the collection when the object gives us the minimum distance and this distance is smaller than a threshold value.

$$d_i = \min \|h - h_i\| \leq J \quad (12)$$

If we have a large collection of objects the best approach is to compute the universal eigenspace which contains all images and all positions. The first step is to recognise the object projecting the input image on this universal eigenspace and after this we can estimate precisely the position by projecting the input image on the object eigenspace.

Certainly the universal eigenspace will be difficult to compute since the number of images for a large collection of objects is huge. For this reason we will compute the largest P eigenvalues and the corresponding eigenvectors. But the advantage in recognition terms is very important because we can determine the object from collection in only one step (see also [2], [5]). The second step is to estimate the position of the object. Otherwise we have to search each object's eigenspace one by one and this method is far from efficient. We can use this approach in case we have a small number of objects or the computation time is not very important for our application.

5. 3-D OBJECT RECOGNITION

We use this approach for our bin picking application. In order to recognise the object and its position in space is necessary to have a depth perception of the scene, allowing the comprehension of 3-D relationship between objects in the real world. For this purpose was developed a depth from defocusing technique, the depth estimation is calculated from the degree of blurring in the two images (more details can be found in [11], [12]).

This transition from 2-D image to 3-D image is presented in figure 4.

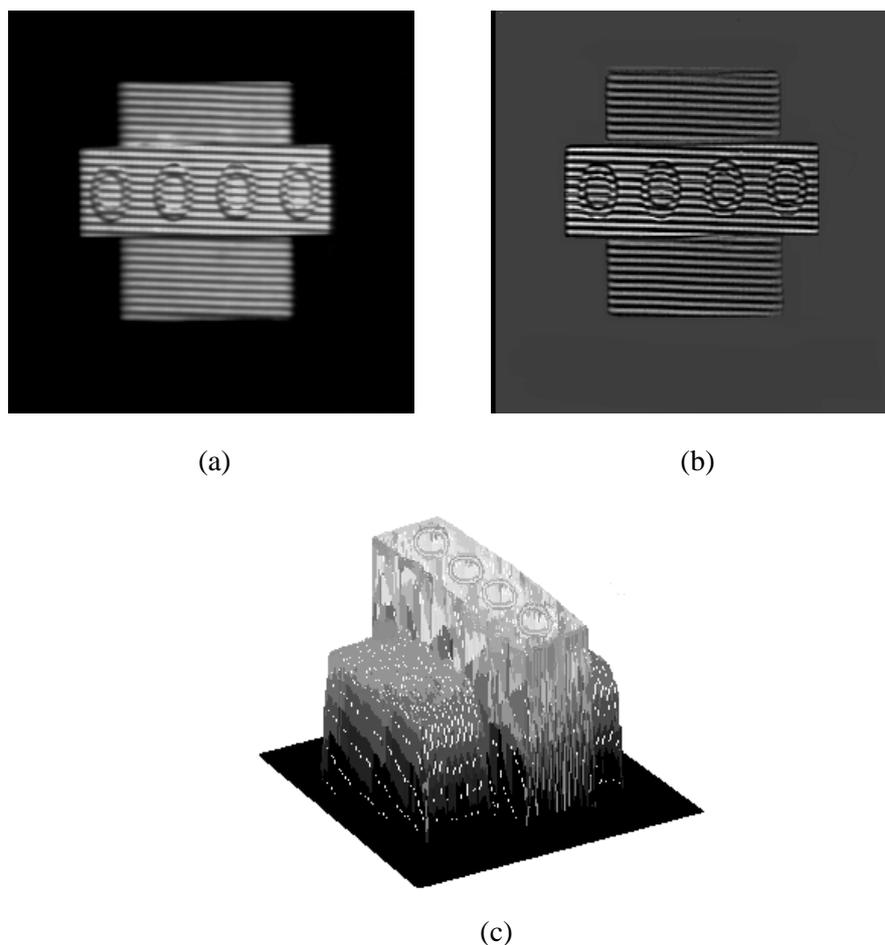


Figure 4. (a) 2-D image, (b) 3-D depth map, and (c) the spatial representation of the 3-D depth map

Certainly in this case it is necessary to construct the universal eigenspace and each objects eigenspace using images corresponding to the depth map. The recognition task remains unchanged by projecting the input image on the eigenspace and compute the Euclidean distance.

6. EXPERIMENTS AND RESULTS

Designing a practical system for object recognition require accuracy and speed. If the number of objects and corresponding positions are small (less than 50), the best implementation is to construct only a universal eigenspace. Clearly this is an approximate position estimation, but suitable for a range of applications. If the accuracy or the number of objects is large we are required to construct the universal eigenspace and the object eigenspace for each object [6]. In our implementation we used both methods. Another key problem is the dimension of the eigenspace. As we discussed before this number is limited to P which is the number of positions for each object. This number can vary from object to object and is in direct connection with the number of objects. For this present algorithm we have obtained poor results if the dimension of the eigenspace is less than 5. We increase the eigenspace dimension to 30 step by step but the rate of recognition is not affected visibly after 15 when the recognition rate is near to 100%.

It is very important to maintain the illumination at a constant level. This requirement is very important especially for 3-D recognition, as the depth map is sensitive to different levels of illumination. For 3-D detection we project a structured light pattern to obtain a better representation of shape. Object reflectance and occlusion can cause errors in the recognition process (more details concerning object reflectance can be found in [9]). If the level of light is not constant for each position, then we have to acquire the same image with different degree of illumination. It is clear that in this case the number of images is huge and to solve this problem is computationally intensive.

As a result we have obtained correct recognition for objects from an image set (universal image set) and position estimation with an error of less than 6 degrees for an object set which contains 36 images. If we use a small number of objects (less than 15) for an object set, the results concerning position estimation are unreliable.

7. CONCLUSIONS

We have presented a possible approach to object recognition for robotic vision applications. In comparison with other methods this implementation is simple, fast and reliable even if it is not a unique solution for recognition problem (also see [3], [4], [14]). It is very important to remember that many applications do not require unity rate of recognition for position and only estimation with a certain error. Furthermore this approach can be easily implemented in hardware for a real time application and the future research will be focused in this direction (for more details see [10], [15], [16]).

Our experiments show that the eigenspace technique can be used for object recognition and position estimation with a very high degree of accuracy. Also a novel approach for 3-D object recognition was briefly presented. All these results prove the robustness and recommend this method for robotic applications.

ACKNOWLEDGEMENTS

This research was supported by Motorola BV, Dublin, Ireland.

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